

AKSHAYA TUTORIALS

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SSLC MATHEMATICS FORMULAE

ARHETMATIC PROGRESSION

- General form of A P
 $a, a + d, a + 2d, a + 3d, \dots$
- Formula to find the common difference
 $d = \frac{a_p - a_q}{p - q}, d = a_2 - a_1, d = a_3 - a_2$
- n^{th} term of an A P is $a_n = a + (n - 1)d$

- Sum of the terms of A P $S_n = \frac{n}{2}(2a + (n - 1)d)$
- Sum of the A P when a -first term and l -last term is

$$\text{given } S_n = \frac{n}{2}(a + l)$$

- Sum of first n natural numbers is given by

$$S_n = \frac{n(n + 1)}{2}$$

- Sum of first even numbers
 $2 + 4 + 6 + \dots + 2n = n(n + 1)$

- Sum of first odd numbers
 $1 + 3 + 5 + \dots + (2n - 1) = n^2$

- Sum of first square terms
 $1^2 + 2^2 + 3^2 + \dots + n^2 = \frac{n(n + 1)(2n + 1)}{6}$

- Sum of first cube terms

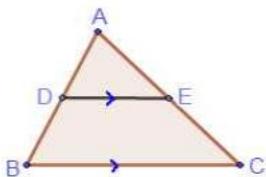
$$1^3 + 2^3 + 3^3 + \dots + n^3 = \left[\frac{n(n + 1)}{2} \right]^2$$

- If a, b, c are in AP then Arhematic mean is given by

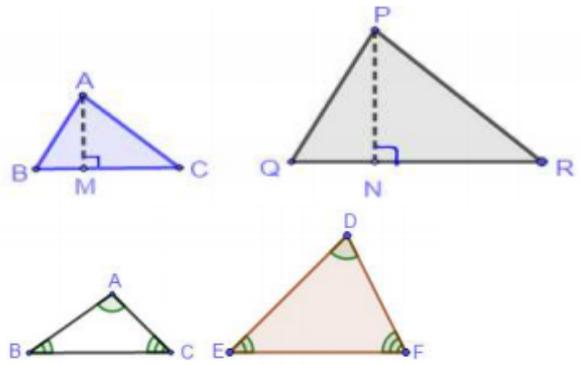
$$b = \frac{a + c}{2}, \text{ where } b \text{ is the A M of } a \text{ and } c$$

TRIANGLES

- Thales theorem $\frac{AD}{DB} = \frac{AE}{EC}$



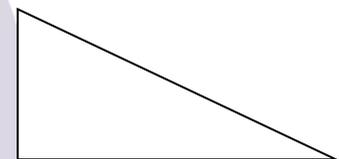
- AAA postulate: if
 $\hat{A} = \hat{D}, \hat{B} = \hat{E}$ and $\hat{C} = \hat{F}$ then



$$\frac{AB}{DE} = \frac{BC}{EF} = \frac{CA}{FD}$$

$$3. \frac{\Delta(ABC)}{\Delta(PQTR)} = \left(\frac{AB}{PQ} \right)^2 = \left(\frac{BC}{QR} \right)^2 = \left(\frac{AC}{PR} \right)^2$$

- Pythagoras theorem: In a right angles triangle the square on the hypotenous is equal to sum of the squares of other two sides



$$AC^2 = AB^2 + BC^2$$

PAIR OF LINEAR EQUATIONS IN TWO VARIABLES

- General form of pair of linear equations

$$a_1x + b_1y + c_1 = 0$$

$$a_2x + b_2y + c_2 = 0$$

If there are two linear equations then condition of them will be given as follows

Condition	Types of solution	Graphical representation	Types of system
$\frac{a_1}{a_2} \neq \frac{b_1}{b_2}$	Unique solution	Intersecting lines	consistent
$\frac{a_1}{a_2} = \frac{b_1}{b_2} = \frac{c_1}{c_2}$	Infinitely many solution	Coinciding lines	consistent
$\frac{a_1}{a_2} = \frac{b_1}{b_2} \neq \frac{c_1}{c_2}$	No solution	Parallel lines	inconsistent

CIRCLES

- The line which touches the circle at only one point is called as tangent

- The tangents drawn from external point to a circle are equal.

AREA RELATED TO CIRCLES

- Circumference $2\pi r$
- Area of a circle πr^2
- The length of the arc which makes an angle θ at the centre is $= \frac{\theta}{360^\circ} \times 2\pi r$
- The area of the sector which makes an angle θ at the centre is $= \frac{\theta}{360^\circ} \times \pi r^2$

CONSTRUCTION

The line drawn from the centre of the circle to the tangent is right angled triangle.

CO - ORDINATE GEOMETRY

- The distance between the two points is defined by $AB = \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2}$

- Distance of a point from the origin is given by

$$OA = \sqrt{x^2 + y^2}$$

- To prove that three points are collinear just prove that $AC = AB + BC$

- Section formula for internal division is defined by

$$(x, y) = \left(\frac{mx_2 + nx_1}{m+n}, \frac{my_2 + ny_1}{m+n} \right)$$

- Section formula for external division is defined by

$$(x, y) = \left(\frac{mx_2 - nx_1}{m-n}, \frac{my_2 - ny_1}{m-n} \right)$$

- The mid point formula is

$$(x, y) = \left(\frac{x_1 + x_2}{2}, \frac{y_1 + y_2}{2} \right)$$

- Area of the triangle formed by the three points (x_1, y_1) , (x_2, y_2) and (x_3, y_3) is given by

$$\Delta = \frac{1}{2} \sum x_1(y_2 - y_3)$$

$$\Delta = \frac{1}{2} [x_1(y_2 - y_3) + x_2(y_3 - y_1) + x_3(y_1 - y_2)]$$

REAL NUMBERS

- Euclidean algorithm is defined by if a divides b then there exists unique q and r such that $b = aq + r$
- Any composite number can be expressed as $n = p^{\alpha_1} \times p^{\alpha_2} \times \dots$
- $LCM \times HCF = a \times b$
- HCF and GCD are same

POLYNOMIALS

- Highest power of the variable is called as degree

Degree	name	General form
0	Constant	a
1	linear	$ax + b = 0$
2	quadratic	$ax^2 + bx + c = 0$
3	cubic	$ax^3 + bx^2 + cx + d = 0$

- Polynomials division algorithm

$$p(x) = g(x)q(x) + r(x)$$

QUADRATIC EQUATIONS

Methods for solving quadratic equations

- Factorization
- Formula
- Graphical

Formula to solve quadratic equation

$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

Nature of roots

$\Delta = b^2 - 4ac$	Nature of roots
$\Delta > 0$	Roots are real and unequal
$\Delta < 0$	Roots are imaginary
$\Delta = 0$	Roots are real and equal

- If α and β are the roots (zeros) of the polynomial then

$$\alpha + \beta = -\frac{b}{a} \text{ and } \alpha\beta = \frac{c}{a}$$

- If α, β and γ are the roots of the polynomial

$$ax^3 + bx^2 + cx + d = 0 \text{ then}$$

$$\alpha + \beta + \gamma = -\frac{b}{a}$$

$$\alpha\beta + \beta\gamma + \gamma\alpha = \frac{c}{a}$$

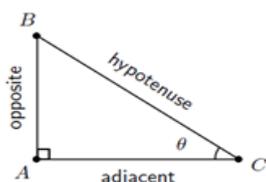
$$\alpha\beta\gamma = -\frac{d}{a}$$

TRIGONOMETRY

Opposite side – which is opposite to θ

Hypogenous- which is opposite to right angle

Adjacent – which is having both θ and side by side



T – function	t- ratio	
$\sin \theta$	$\frac{opp}{hyp}$	$\frac{AB}{BC}$
$\cos \theta$	$\frac{adj}{hyp}$	$\frac{AC}{BC}$
$\tan \theta$	$\frac{opp}{adj}$	$\frac{AB}{AC}$
$\cos ec \theta$	$\frac{hyp}{opp}$	$\frac{BC}{AB}$
$\sec \theta$	$\frac{hyp}{adj}$	$\frac{BC}{AC}$
$\cot \theta$	$\frac{adj}{opp}$	$\frac{AC}{AB}$

Trigonometric standard angles

	0°	30°	45°	60°	90°
$\sin \theta$	0	$\frac{1}{2}$	$\frac{1}{\sqrt{2}}$	$\frac{\sqrt{3}}{2}$	1
$\cos \theta$	1	$\frac{\sqrt{3}}{2}$	$\frac{1}{\sqrt{2}}$	$\frac{1}{2}$	0
$\tan \theta$	0	$\frac{1}{\sqrt{3}}$	1	$\sqrt{3}$	ND
$\cos ec \theta$	ND	2	$\sqrt{2}$	$\frac{2}{\sqrt{3}}$	1
$\sec \theta$	1	$\frac{2}{\sqrt{3}}$	$\sqrt{2}$	2	ND
$\cot \theta$	ND	$\sqrt{3}$	1	$\frac{1}{\sqrt{3}}$	0

Trigonometric complimentary angles

$\sin(90 - \theta) = \cos \theta$	$\cos ec(90 - \theta) = \sec \theta$
$\cos(90 - \theta) = \sin \theta$	$\sec(90 - \theta) = \cos ec \theta$
$\tan(90 - \theta) = \cot \theta$	$\cot(90 - \theta) = \tan \theta$

Trigonometric reciprocal function

$\sin \theta \cdot \cos ec \theta = 1$	$\sin \theta = \frac{1}{\cos ec \theta}$	$\cos ec \theta = \frac{1}{\sin \theta}$
$\cos \theta \cdot \sec \theta = 1$	$\cos \theta = \frac{1}{\sec \theta}$	$\sec \theta = \frac{1}{\cos \theta}$
$\tan \theta \cdot \cot \theta = 1$	$\tan \theta = \frac{1}{\cot \theta}$	$\cot \theta = \frac{1}{\tan \theta}$

Trigonometric quotient relation

$\tan \theta = \frac{\sin \theta}{\cos \theta}$	$\cot \theta = \frac{\cos \theta}{\sin \theta}$
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Trigonometric identities

$\sin^2 \theta + \cos^2 \theta = 1$
$1 + \tan^2 \theta = \sec^2 \theta$
$1 + \cot^2 \theta = \cos ec^2 \theta$

The mean for grouped data can be found by

Method	formula
Direct method	$\bar{x} = \frac{\sum f_i x_i}{\sum f_i}$
Assumed mean method	$\bar{x} = a + \frac{\sum f_i d_i}{\sum f_i}$
Step deviation method	$\bar{x} = a + \frac{\sum f_i u_i}{\sum f_i} \times h$
The mode of grouped data can be found by	$l + \left[\frac{f_1 - f_0}{2f_1 - f_0 - f_2} \right] \times h$
The median for grouped data can be found by using the	$l + \left[\frac{\frac{n}{2} - cf}{f} \right] \times h$

STATISTICS

PROBABILITY

1. All possible outcome set is called as sample space
2. Any possible outcomes are called as event denoted by E
3. Probability always lies between 0 and 1
4. Probability of sure event is 1
5. Probability of impossible event is 0
6. Probability is defined as

$$p(A) = \frac{\text{no of favourable outcomes}}{\text{total no outcomes}} = \frac{p(E)}{p(S)}$$

7. For any event $p(E) + p(\bar{E}) = 1$, where E is the event and \bar{E} is not E

SURFACE AREA AND VOLUME

NAME OF THE SOLID	FIGURE	VOLUME	CURVED SURFACE AREA	TOTAL SURFACE AREA
CUBOID		lbh	$2h(l + b)$	$2(lh + bh + hb)$
CUBE		a^3	$4a^2$	$6a^2$
RIGHT CIRCULAR CYLINDER		$\pi r^2 h$	$2\pi r h$	$2\pi r(h + r)$
RIGHT CIRCULAR CONE		$\frac{1}{3} \pi r^2 h$	$\pi r l$	$\pi r(l + r)$
SPHERE		$\frac{4}{3} \pi r^3$	$4\pi r^2$	$4\pi r^2$
HEMISPHERE		$\frac{2}{3} \pi r^3$	$2\pi r^2$	$3\pi r^2$